



Basic Biostatistics

Section Three



Our clinical example:

- ◆ Our prior testing revealed that Drug B is better than Drug A.
 - Should I change my practices and prescribe this new drug?
- ◆ What test should be used to compare the data and aid me in answering the question?



Choosing the appropriate test

- ◆ Based on the two aspects of the data
 - Types of variables
 - Remember Day 1 with dependent and independent variables and the categories (discrete/ continuous)
 - Number of groups being compared
 - Most common questions compare two groups (dead/alive, treated/untreated, diseased/non-diseased, drug A/ drug B)
 - If the wrong test is used false conclusions can be reached

A quick review

◆ Discrete

- Nominal
 - Dead/Alive, race, marital status
- Ordinal
 - Stage of cancer, rating systems for disease i.e. heart failure or burns

◆ Continuous

- Ratio
 - Age, BP, Cholesterol, Height
- Interval
 - Quality of life, mental status exam scores, IQ





Signal to Noise

a funny statistician's term

- ◆ Standard Deviation reflects the variation of individual values around the sample mean
- ◆ Standard Error reflects the variation of many sample means from the same size samples around the true population means.
 - Standard error is always smaller than Standard Deviation.
 - Studies use multiple centers each with their own subset of data to compare to the larger sample.



Discrete/Categorical Data

- ◆ **Chi Square test** for sample size greater than 30 or no less than 5 in any combination
 - If not greater than 30, then **Fisher's Exact Test**
 - Assumes all patients are independent
 - Based on frequencies, not percents
- ◆ Results tell us if distributions are different but not the magnitude or any clinical significance
 - Group A and Group B are not the same population
 - Can not differentiate how different



Our question

Drug Group	Glycemic Control achieved	Glycemic Control not achieved
Drug A	300	80
Drug B	170	180

The Chi Square statistic for this table is 73.31 and corresponds to a p value of 0.001, available in a table. This is less than our usual 0.05 and we then reject the null hypothesis and accept that patients on Drug A achieve glycemic control at a different rate than those on Drug B, the means infer that A is superior.



For two independent groups with a continuous variable

◆ Student's T-Test

- Compares the difference in the means of two groups divided by the standard error
- The higher the difference and the smaller the standard error the more likely the result will be significant
- If the groups are not independent then a paired t-test is used (the groups are related in some way other than the variables in your study)
 - **Pre/ Post treatment**
 - **Eyes**
 - **Twins**



In our example

- ◆ Change the variable now Drug A and the mean blood glucose with a standard deviation
 - Compared to...
- ◆ Drug B and the mean blood glucose with a standard deviation

- ◆ We can now see the difference as a continuous number (the difference of the means divided by the standard error)



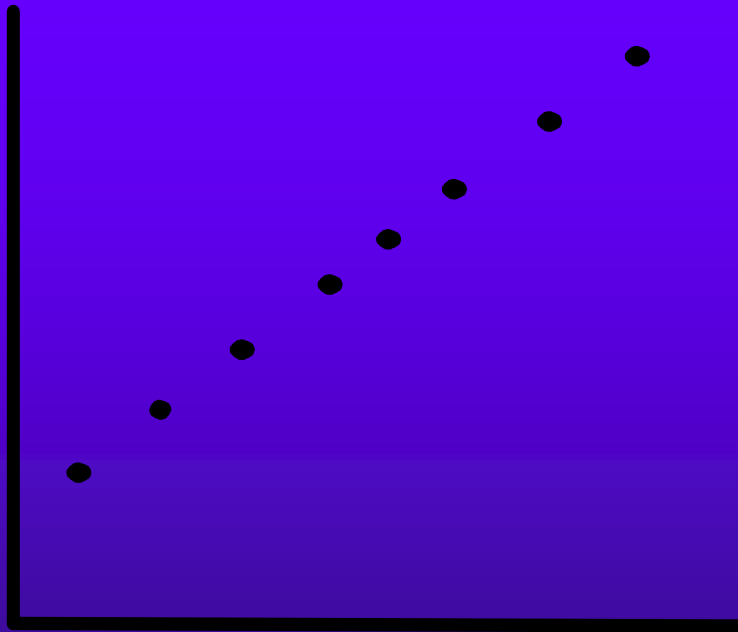
Correlation Coefficient

- ◆ Defined as r
- ◆ Describes the tightness of the data points around the best fit line
 - $r = 1$ is perfect positive correlation (all the dots line up in a straight line with a positive slope)
 - $r = -1$ is perfect negative correlation (all the dots line up in a straight line with a negative slope)
 - $r > 0.7$ is good, 0.5 to 0.7 is moderate and < 0.5 is weak
 - If you are looking for a negative correlation then the values are negative for r



Perfect Positive Correlation

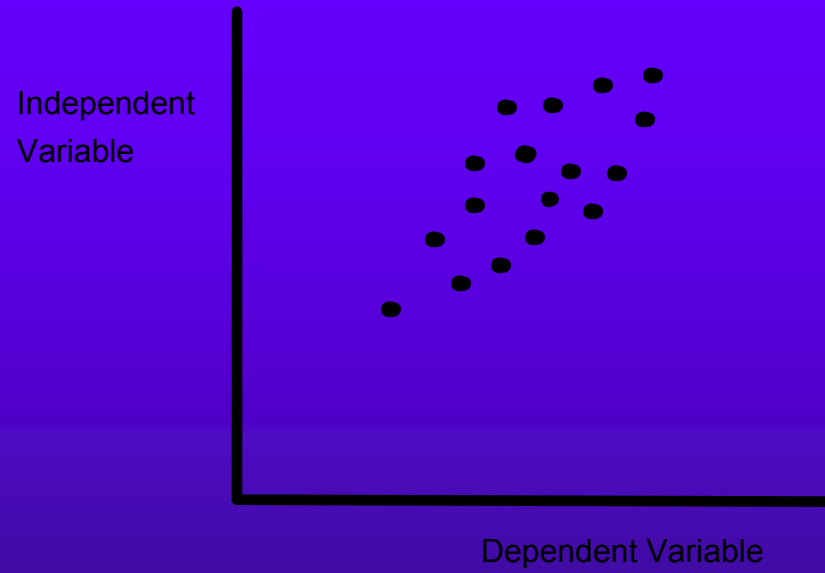
Independent
Variable



Dependent Variable



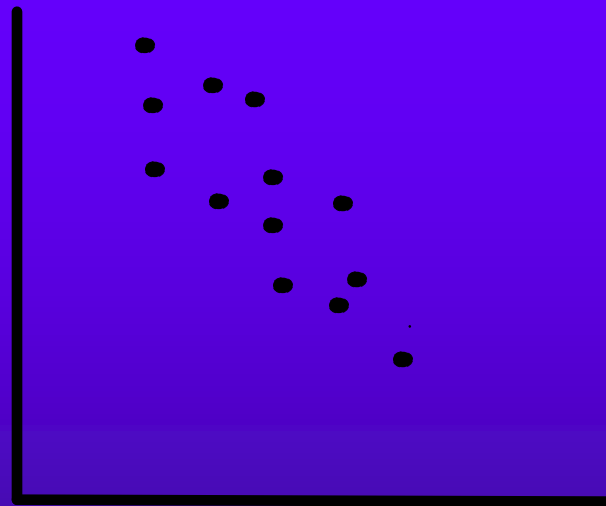
Weak Positive Correlation



Strong Negative Correlation



Independent
Variable

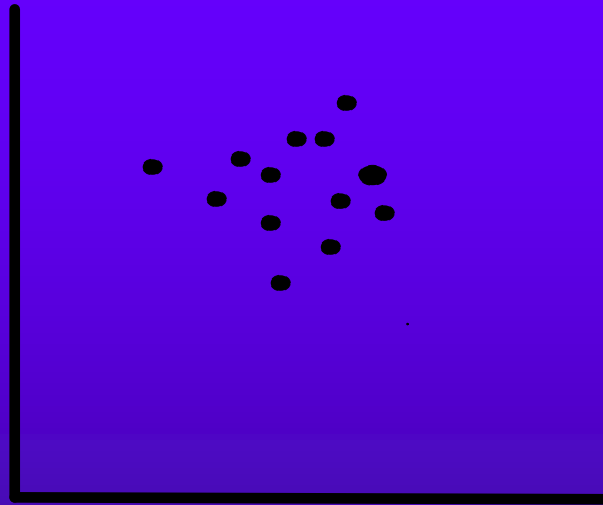


Dependent Variable

Nonexistent (Zero) Correlation



Independent
Variable



Dependent Variable



Pitfalls

- ◆ Correlation does not yield causation
 - Just because they are related does not mean that one causes another (coffee consumption is related to lung cancer but there is no known causal relationship)
- ◆ Correlation Coefficient squared r^2 is the amount of variance in X (the dependent variable) explained by Y (the independent variable)
 - How much of the outcome is X can be related to Y
 - Example: How much of the rate of lung cancer can be related to tobacco use (packs/day)
- ◆ The slope of the line describes the degree of the relationship
 - Back to geometry $y=bx + a$



How you use this:

- ◆ The slope (b) describes that a specific change in X that will a specific change in Y
- ◆ A p-value also exists for the slope
- ◆ $Y = bX + A$
 - b is the slope
 - b relates to r by the standard deviation
 - Each increase in packs per day causes what increase in the rate of Lung Cancer



So, finally back to our question

- ◆ In our patient with mild type II diabetes is Drug A better than Drug B and if so by how much?
 - One step closer to clinical relevance
 - Confidence Intervals



Confidence Intervals

- ◆ Another approach to p-values
- ◆ Provides a range in which we are 95% confident the true population parameter lies.
- ◆ We accept that there is a 5% chance that the real value is not in our range
- ◆ It could be comparing 2 means, odds ratios, relative risks, response rates, etc...

Confidence Intervals

◆ Important:

- The interval states we are 95% sure that the real value is in our range

NOT

- 95% of the time the value is in our range

or

- 5% of the time our mean value is wrong





Confidence Intervals

Constructed in the formula

Sample estimate (mean, difference between means, mortality rate, odds ratio)

\pm Z score for confidence
x (Standard Error)

i.e. 100 ± 5 95% CI: (95,105)

we are 95% sure that the real value is between 95 and 105



Z score and Standard Error

- ◆ The Z score is actually based on 97.5% (2.5 SD) because the 5% need to be divided on both ends of range this is 1.96
- ◆ The Standard Error is the standard deviation divided by the square root of sample size



Clinical Utility

- ◆ A confidence interval is reported for each value and if they do not overlap we can conclude with 95% confidence that they are different
- ◆ The difference can also be compared and given a confidence interval and if it doesn't cross zero you can conclude that the difference is significant and gives you a range that the difference could occur it
- ◆ An increase in power will decrease the size of the CI.



Now a new study compares

- ◆ Sugarlow to Glucobust for the treatment of Type II diabetes and reports the mean blood glucose of patients in each treatment arm
 - Sample size = 50
 - Sugarlow = 92 ± 8
 - Glucobust = 103 ± 12



Now a new study compares

◆ Sugarlow

- 92 ± 8
- $92 \pm 1.96(8/\sqrt{50})$
- 92 ± 2.2
- 95% CI: (89.8,94.2)

◆ Glucobust

- 103 ± 12
- $103 \pm 1.96(12/\sqrt{50})$
- 103 ± 3.3
- 95% CI: (99.7,106.3)

Since the two intervals do not overlap the population differences are statistically significant.



One step more

- ◆ The difference in the values can also be compared
 - $103 - 92 = 11$
 - Trust me the standard error is 2
 - If you want to know.... Read Studying a Study in the recommended readings.
 - 11 ± 2 CI: (9,13)

Finally!

- ◆ We are 95% certain the difference is between 9 and 13
- ◆ Now for the clinician's interpretation
 - The difference could be 9
 - Worst case scenario
 - The difference could be 13
 - Best case scenario
- ◆ Is this difference clinically useful?
 - Still up to the individual clinician!
 - But you can be confident in what you decide
 - Evidence Based Medicine in a nutshell

